ST JOSEPH’S UNIVERSITY
BENGALURU-27

DEPARTMENT OF MATHEMATICS

SYLLABUS FOR POSTGRADUATE PROGRAMME

For Batch 2024-2026

PART A

1	Title of the Academic Program	M.Sc Mathematics	
2	Program Code	**(To be given by Examination Section)**	
3	Name of the College	St. Joseph's College (Autonomous)	
4	Objective of the College	1. Academic Excellence 2. Character Formation 3. Social Concern	
5	Vision of the College	"Striving for a just, secular, democratic and economically sound society, which cares for the poor, the oppressed and the marginalized"	
6	Mission of the College	**M1**	St. Joseph's College (Autonomous) seeks to form men and women who will be agents of change, committed to the creation of a society that is just, secular and democratic.
		M2	The education offered is oriented towards enabling students to strive for both academic and human excellence.
		M3	The college pursues academic excellence by providing a learning environment that constantly challenges the students and supports the ethical pursuit of intellectual curiosity and ceaseless enquiry.
		M4	Human excellence is promoted through courses and activities that help students achieve personal integrity and conscientise them to the injustice prevalent in society.
7	Name of the Degree	Master of Science (M.Sc.) in Mathematics	
8	Name of the Department offering the program	Mathematics	
9	Vision of the Department offering program	"The Department endeavors to be a center of excellence nurturing joyful curiosity in learning, enthusiastic creativity in research, passion to build a free, transparent and dynamic teaching learning community with a commitment to share and serve."	
10	Mission of the Department offering program	• Initiating students in the use of the power of abstraction. • Enable students to perceive, enjoy and create patterns and the relationships that underlie the structures of Mathematics. • Teach students to pose and solve meaningful Mathematical problems that delve into the service of humanity.	
11	Duration of the Program	Two years (Four semesters)	
12	Total No. of Credits	Ninety Six	
13	Program Educational Objectives (PEOs)	**PEO 1**	The M.Sc programme is meticulously designed to impart essential knowledge in Mathematics with opportunities for specialization in all major areas of pure and applied mathematics as well as pursuing academic/industrial careers.

		PEO 2	The non-academic outreach activities associated with the programme aim to inculcate in students a basic sense of responsibility and empathy towards social issues.
		PEO 3	The teaching methodology (which focuses on the "why" rather than the "what"), adopted by faculty will instill a life-long learning attitude among students, to adopt new skills and techniques that will help overcome the problems that evolve with changing times.
		PEO 4	The teaching pedagogy will encourage students to engage in an active learning process.
14	Graduation Attributes		The Following graduate attributes reflect the particular quality and feature or characteristics of an individual, that are expected to be acquired by a graduate through studies at St. Joseph's College. ● **Disciplinary knowledge** ● **Critical thinking** ● **Problem solving** ● **Analytical reasoning** ● **Research-related skills** ● **Cooperation/Teamwork** ● **Reflective thinking** ● **Self-directed learning and Lifelong learner** ● **Moral and ethical awareness/reasoning**
15	Program Outcomes (POs)	**PO1**	Students would have developed the ability to formulate and structure mathematical arguments through logical and deductive thinking.
		PO2	Students would be competent in using programming languages like Python/ SageMath/R programming to solve problems related to the latest mathematical and industrial research.
		PO3	Students would be able to work well as a team.
		PO4	Students would be aware of their moral obligations to society and be willing to involve in tasks that work towards the greater good.

PART B

M.Sc. Mathematics Curriculum

Courses and course completion requirements	No. of credits
Mathematics	94
Outreach activity and Ignitors	04

SUMMARY OF CREDITS

DEPARTMENT OF MATHEMATICS (PG) (2022-2024)								
Semester 1	**Code Number**	**Title**	**No. of Hours of Instructions**	**Number of Hours of teaching per week**	**Number of credits**	**Continuous Internal Assessment (CIA/PIA) Marks**	**End Semester Marks**	**Total marks**
Theory	MT 7121	Algebra I	60	04	04	50	50	100
Theory	MT 7221	Real Analysis	60	04	04	50	50	100
Theory	MT 7321	Linear Algebra	60	04	04	50	50	100
Theory	MT 7424	Ordinary Differential Equations	60	04	04	50	50	100
Theory	MT 7524	Discrete Mathematics and Graph Theory	60	04	04	50	50	100
Practical	MT 7P124	Linear Algebra and ODE with SageMath	44	04	02	25	25	50
Practical	MT 7P224	Graph Theory with SageMath	44	04	02	25	25	50
Total Number of credits:					**24**			

Semester 2	Code Number	Title	No. of Hours of Instructions	Number of teaching hours /week	Number of credits	Continuous Internal Assessment (CIA) Marks	End Semester Marks	Total marks
Theory	MT 8121	Algebra II	60	04	04	50	50	100
Theory	MT 8221	Measure and Integration	60	04	04	50	50	100
Theory	MT 8325	Complex Analysis	60	04	04	50	50	100
Theory	MT 8421	Partial Differential Equations	60	04	04	50	50	100
Theory	MT 8521	Topology	60	04	04	50	50	100
Theory	MT 8624	Probability and Statistics	60	04	04	50	50	100
Practical	MT 8P24	Probability and Statistics with R Programming	44	04	02	25	25	50
Total Number of credits:					**26**			
Semester 3	**Code Number**	**Title**	**No. of Hours of Instructions**	**Number of teaching hours /week**	**Number of credits**	**Continuous Internal Assessment (CIA) Marks**	**End Semester Marks**	**Total marks**
Theory	MT 9122	Functional Analysis	60	04	04	50	50	100
Theory	MT 9225	Classical and Continuum Mechanics	60	04	04	50	50	100
Theory	MTDE 9322 OR MTDE 9425	Graphs and Matrices OR Optimization Techniques	60	04	04	50	50	100

Theory	MT 9525	Mathematical Methods	45	03	03	50	50	100
Students may choose an NPTEL (SWAYAM) course of 3 credits from among PG level Mathematics courses, instead of MT 9525. Approval to take such a course is subject to the decision of the advisory committee set up by the PG co-ordinator.								
Theory	MT 9625	Numerical Analysis	60	04	04	50	50	100
Practical	MT 9P25	Numerical Analysis with SageMath	44	04	02	25	25	50
Project	MT 9R125	Introduction to Mathematical Research	33	03	02	NA	NA	50
Total Number of credits:				**23**				
Semester 4	**Code Number**	**Title**	**No. of Hours of Instruction**	**No. of teaching hours a week**	**Number of credits**	**Continuous Internal Assessment (CIA) Marks**	**End Semester Marks**	**Total marks**
Theory	MT 0125	Differential Geometry	60	04	04	50	50	100
Theory	MT 0222	Fluid Mechanics	60	04	04	50	50	100
Theory	MT 0325	Applied Stochastic Processes	45	03	03	50	50	100
Students may choose an NPTEL (SWAYAM) course of 3 credits from among PG level Mathematics courses, instead of MT 0325. Approval to take such a course is subject to the decision of the advisory committee set up by the PG co-ordinator.								
Theory	MTDE 0425 OR MTDE 0525	Advanced Graph Theory OR Number Theory	60	04	04	50	50	100
Project	MT9R225	Project	22	02	06	NA	NA	150

		IGNITORS/ OUTREACH						
Total Number of credits:				**21**				
Total No. of Credits : 94								
Method of evaluation of MT9R125 and MT9R225 is mentioned along with the syllabus of all courses.								

CORE COURSES (CC)	
Course Title	**Code Number**
Algebra I	MT 7121
Real Analysis	MT 7221
Linear Algebra	MT 7321
Ordinary Differential Equations	MT 7424
Discrete Mathematics and Graph Theory	MT 7524
Algebra II	MT 8121
Measure and Integration	MT 8221
Complex Analysis	MT 8325
Partial Differential Equations	MT 8421
Topology	MT 8521
Statistics	MT 8624
Functional Analysis	MT 9122
Classical and Continuum Mechanics	MT 9225
Mathematical Methods	MT 9525
Numerical Analysis	MT 9625
Differential Geometry	MT 0125
Fluid Mechanics	MT 0222
Applied Stochastic Processes	MT 0325

DISCIPLINE SPECIFIC ELECTIVE COURSES (DSE)	
Course Title	**Code Number**
Graphs and Matrices	MTDE 9322
Optimization Techniques	MTDE 9425
Advanced Graph Theory	MTDE 0425
Number Theory	MTDE 0525

SKILL ENHANCEMENT COURSE (SEC)	
Course Title	**Code Number**
Linear Algebra and ODE with SageMath	MT 7P124
Graph Theory with SageMath	MT 7P224
Statistics with R programing	MT 8P24
Numerical Analysis with SageMath	MT 9P125
Introduction to Mathematical Research	MT 9R125
Project	MT 9R225

Course Outcomes and Course Content
Semester I

Semester	I
Paper Code	**MT 7121**
Paper Title	**Algebra I**
Number of teaching hours per week	04
Total number of teaching hours per semester	60
Number of credits	04

Objective of the Paper:
To learn the concept of group action and use it to deduce important theorems in group theory regarding Class Equation, Automorphism, Inner Automorphism, Sylow's Theorem and other standard results. To understand the concept of irreducibility of polynomials. To understand the concepts of Euclidean Domain (ED), Principal Ideal Domain (PID) and Unique Factorization Domain (UFD).

Syllabus:

Unit 1
A few examples of groups: Dihedral Groups, Symmetric Groups, Matrix Groups, Quaternion Groups.
Group actions: Revisiting Cosets and Lagrange's theorem , Example showing that the converse of Lagrange's theorem is not true. Definition of group action and examples, Permutation representations. Cayley's Theorem and its generalization, A subgroup of index p where p is the smallest prime dividing the order of the group is normal, Group Acting on themselves by Conjugation, Class Equation, Conjugacy in Symmetric Group, A_5 is a simple group.

(15 hours)

Unit 2
Automorphisms: Automorphism group (Aut(G)), The quotient of a group by its center is isomorphic to a subgroup of Aut(G), Inner automorphism group, Computing Automorphism groups and Inner Automorphism groups, The automorphism group of finite cyclic group, Giving explicit descriptions of Automorphism groups.
Sylow's Theorem: Definition of p-subgroup, Sylow- p subgroup. Sylow's Theorem. Application of Sylow's Theorem: Groups of order pq, Groups of order 30, Groups of order 12, Groups of order p^2q, Groups of order 60. Simplicity of Alternating Group. Any simple group of order 60 is isomorphic to A_5. A_n **is simple for** $n \geq 5$**.** Sylow subgroups of D_{2n}, S_n A_n, $SL_n((F_p)$, and

problems from Exercise 4.5 (Page-146) from the main reference book that is Abstract Algebra by Dummit and Foote.

External Direct Product: Definition and examples of external direct products. Properties of external direct products.

Fundamental Theorem of Abelian Group: The fundamental theorem of finite abelian groups (without proof) and related problems. Greedy algorithm and related problems. Isomorphism classes of finite abelian groups. The fundamental theorem of finitely generated abelian groups (without proof).

(20 hours)

Unit 3:

Polynomials Rings and Factorization of Polynomial Rings: Polynomial ring, D[x] is an integral domain if D is an integral domain, Division algorithm. Remainder Theorem. Factor Theorem. Polynomials of degree n has at most n zeros counting multiplicity. Principal Ideal Domain (PID, If F is a field then F[x] is a PID.

Irreducible and Reducible Polynomial. Reducibility Test for Degree 2 and 3 polynomials, Gauss. Primitive polynomial. Content of a polynomial. Gauss lemma. Mod-p irreducibility Test, Eisenstein's criterion. Cyclotomic Polynomial. Constructing fields with p^n elements, where p is a prime and n is an integer.

(13 hours)

Unit 4:

Euclidean Domains(ED), Principal Ideal Domains(PID) and Unique Factorization Domain(UFD):

Definition and Examples of ED, Non-Examples: $Z[x]$,$Z[\sqrt{-5}]$, Concept of Greatest Common Divisor(GCD), Algorithm to find GCD of two elements in a ED, Definition and Examples of PID, Non-Examples: $Z[x]$,$Z[\sqrt{-5}]$, GCD in a PID, Every nonzero prime ideal is a maximal ideal, If $R[x]$is a PID then R is a field, Definition of irreducible and prime elements, In an integral domain a prime element is always irreducible. In a PID an element is prime iff it is irreducible, Definition and Examples of UFD, GCD of two elements in a UFD.

Every ED is a PID, In a UFD a nonzero element is prime if and only if it is irreducible. Every PID is a UFD.

(12 hours)

TEXT BOOKS:

1. D. S. Dummit and R. M. Foote. Abstract Algebra. Wiley. 2003.
2. J. A. Gallian. Contemporary Abstract Algebra. 4th Edition. Narosa Publishing. 2011.

REFERENCE BOOKS:

1. C. S. Musili. Rings and Modules . 2nd Revised Edition. Narosa Publishing House. 1994.
2. I. N. Herstein. Topics in Algebra. 2nd Edition. Wiley. 1975.
3. I. S. Luthar and I. B. S. Passi. Algebra Volume-I Groups. Narosa Publishing House. 2013.
4. I. S. Luthar and I. B. S. Passi. Algebra Volume-II Rings. Narosa Publishing House. 2013.
5. J. B. Fraleigh. A first course in Abstract Algebra. 7th Edition Pearson Education India 2002.
6. M. Artin . Algebra. 2nd Edition Pearson Education India. 2017.

7. S. K. Mapa. Higher Algebra Abstract and Linear. Sarat Book House. 1972.
8. S. Lang. Algebra. 3rd Edition. Springer. 2002.

QUESTION PAPER PATTERN:

Code number: MT 7121

Title of the paper: ALGEBRA I

Paper Pattern: Students will have to answer 5 out of 7 main questions. Each main question will be worth a total of 10 marks.

The end semester question paper will have a weightage of 35% of the questions from the first half of the syllabus (the portions covered for the mid-semester examination) and a weightage of 65% of the questions from the second half of the syllabus (the portions not covered for the mid-semester examination).

Course Outcomes: At the end of the Course, the Student should

CO1	Have developed good knowledge of Sylow's Theorems and irreducibility test for polynomials . Know the relation between ED, PID and UFD and different examples of them.
CO2	Understand the proofs of Sylow's Theorem, Fundamental Theorem of Abelian Group and the various irreducibility tests of polynomials.
CO3	Be able to apply Sylow's theorem to various problems in group theory, specially to check whether a group is simple and also to classify groups of certain orders. Be able to check the irreducibility of polynomials. Be able to check the nature (ED/PID/UFD) of a domain.
CO4	Be able to analyse which method of solution is the easiest to solve a given problem.
CO5	Be able to critique various proof methods for a particular theorem and explain why (or why not) one way is more useful than the other.
CO6	Be able to create examples and counter-examples particularly when working with the converse of certain theorems and implications.

Semester	**I**
Paper Code	**MT 7221**
Paper Title	**Real Analysis**
Number of teaching hours per week	04
Total number of teaching hours per semester	60
Number of credits	04

Objective of the Paper:
To comprehend the basics of Riemann Integration, improper integration and Sequences and Series of functions. To understand the fundamental concepts of metric spaces.

Syllabus:

Unit 1:
Countability: Finite, Infinite, Denumerable, Countable, Uncountable sets. Examples, non-examples and properties of these sets. Countable union of countable sets is countable. The real line is uncountable. Cardinality of sets and related results. Cantor's Theorem.

(8 hours)

Unit 2:
Riemann Integration: Partition of a closed bounded interval. Upper and lower Darboux sums and Darboux integrals. Examples of integrable and non-integrable functions. Criteria for integration. Continuous and monotonic functions are integrable. Squeeze theorem. Riemann sums and Riemann definition of integral. Equivalence of the two definitions. Properties of Riemann integral. Lebesgue criterion. Indefinite integral. Fundamental theorems of calculus and mean value theorems. Integration by parts.

(18 hours)

Unit 3:
Sequence and Series of Functions: Pointwise convergence of sequence of functions. Different examples. Uniform convergence. Necessary sufficient conditions for uniform convergence. Uniform convergence and continuity. Uniform convergence and integration. Uniform convergence and differentiation. Weierstrass Approximation Theorem (without proof) and related problems. Power series. Radius of convergence.

(12 hours)

Unit 4:
Metric Spaces: Notion of a metric space and examples. Open and closed sets in a metric space. Interior, exterior and boundary point. Limit and cluster point. Closure of sets. Bounded sets.

Distance between sets. Diameter of a set. Cantor's Intersection Theorem and its converse.

Complete Metric spaces: Sequences and subsequences in a metric space. Convergence of sequences in a metric space. Cauchy sequences in a metric space. Complete metric spaces. Subspaces of complete metric spaces. First and second category spaces. Baire's category theorem and its applications.
Continuous functions on metric spaces: Real valued continuous functions. Continuous functions between arbitrary metric spaces. Equivalent definitions of continuity. Examples of continuous functions. Uniform continuity.

(22 hours)

TEXT BOOKS:

1. S. K. Mapa. Introduction to Real Analysis. 7th Edition. Sarat Book House. 2013.
2. D. R. Sherbert and G. Bartle. Introduction to Real Analysis. 4th Edition. Wiley. 2014.
3. D. Gopal, A. Deshmukh, A. S. Ranadive and S. Yadhav. An Introduction to Metric Spaces. 1st Edition. CRC Press. 2021.

REFERENCE BOOKS:

1. W. Rudin. Principles of Mathematical Analysis. 3rd Edition. McGraw-Hill Education.1976
2. J. M. Howie. Real Analysis. Springer India. 2001
3. S. K. Berberian. A first course in Real Analysis. Springer India. 1994
4. S. R. Ghorpade and B. V. Limaye. A course in Calculus and Real Analysis. 1st Edition. Springer. 2006
5. S. Shirali and H. L. Vasudeva. Metric Spaces. Springer. 2006
6. C. C. Pugh. Real Mathematical Analysis. 2nd Edition. UTM Springer. 2002
7. G. F. Simmons. Introduction to Topology and Modern Analysis. Tata McGraw-Hill Edition. 2004
8. S. Kumaresan. Topology of Metric Spaces. 2nd Edition. Narosa. 2005.
9. J. Munkres. Topology. 3rd Edition. PHI Learning Limited. 2012.

QUESTION PAPER PATTERN
Code number: MT 7221
Title of the paper: REAL ANALYSIS
Paper Pattern: Students will have to answer 5 out of 7 main questions. Each main question will be worth a total of 10 marks.
The end semester question paper will have a weightage of 35% of the questions from the first half of the syllabus (the portions covered for the mid-semester examination) and a weightage of 65% of the questions from the second half of the syllabus (the portions not covered for the mid-semester examination).

Course Outcomes: At the end of the Course, the Student should

CO1	Have good knowledge of the development of Riemann integration. Know the

	significance of uniform convergence over pointwise convergence of sequences/series of functions. Know examples and properties of finite, infinite, countable and uncountable sets as well as metric spaces.
CO2	Understand the geometry involved in the construction of the Riemann integral and in convergence. Understand the different techniques for checking if a given function is a metric and if a given set is countable/uncountable or open/closed.
CO3	Be able to apply the theorems learnt in each topic to solve problems.
CO4	Be able to analyze which method of solution is the easiest to solve a given problem.
CO5	Be able to critique various proof methods for a particular theorem and explain why (or why not) one way is more useful than the other.
CO6	Be able to create examples and counter-examples particularly when working with the converse of certain theorems and implications.

Semester	I
Paper Code	**MT 7321**
Paper Title	**Linear Algebra**
Number of teaching hours per week	04
Total number of teaching hours per semester	60
Number of credits	04

Objective of the Paper:
To study the general theory of vector spaces and linear transformations and understand different ways for representing linear transformations in simpler ways by means of matrices. To study vector spaces with some extra structures like inner product spaces, endomorphism rings, and some special type of linear transformations on some of these spaces like adjoint transformations, self-adjoint transformations, orthogonal transformations etc.

Syllabus:

Unit 1:
Vector spaces: Review of solving system of equations and motivation for vector space structure on R^n. Abstract Vector spaces – Definition and examples. Subspaces – Criterion for a subset to be a subspace, Examples, Union and Intersection of subspaces, Subspace generated by a set. Basis and dimension – Linear dependence and Independence, Definitions of a finite dimensional space, Basis and Dimension, Criterion for a subset to be a basis, Dimension of familiar subspaces. Linear transformations – Basic results, The rank-nullity theorem (Statement only), Algebra of linear transformations. Quotient spaces and the first Isomorphism Theorem (Statement only). Direct sum – Definition of internal direct sum and finding the dimension of direct sum of subspaces. Projection on a subspace along another subspace, The Idempotent operators. The matrix of a linear transformation.

(15 hours)

Unit 2:
Canonical forms: Eigenvalues and eigenvectors – Definitions and basic results. The characteristic and minimal polynomials, Primary decomposition theorem, Annihilating polynomials, Cayley-Hamilton theorem, Computing minimal polynomials of some specific operators. Diagonalizable and Triangulable operators – Criteria for diagonalization and triangularebility. The Jordan form – The generalized eigenvectors and eigenspaces, The main theorem on Jordan canonical forms (Statement only), Problems on computing Jordan forms.

(20 hours)

Unit 3:

Inner Product Spaces: Inner products. Orthogonality. The Gram-Schmidt Orthogonalization Process. Orthogonal Complement. Adjoint of a linear operator. Self-adjoint and Normal operators. Unitary and Orthogonal matrices and Operator. Positive definite matrices. Test for positive definiteness. Polar and Singular value decomposition.

(20 hours)

Unit 4:

Bilinear forms and Quadratic forms: Bilinear forms and Quadratic forms - Definitions and Examples. The matrix of a bilinear form and problems. **(5 hours)**

TEXT BOOKS:

1. Vivek Sahai and Vikas Bist : Linear Algebra. 2nd Edition. Narosa Publishing House. 2013.
2. G. Strang : Linear Algebra and Its Application. 4th Edition. Cengage Learning. 2006.

REFERENCE BOOKS:

1. A.R. Rao and P.Bhimasankaram : Linear Algebra. Hindustan Book Agency. Second Edition. 19 TRIM Series. 2010.
2. S. K. Mapa : Higher Algebra Abstract and Linear. revised 9th Edition. Sarath Book House. 2003.
3. A. J. Insel, L. E. Spence and S. Friedberg: Linear Algebra. 4th Edition. Pearson Education. 2003.
4. C. W. Curtis : Linear Algebra an Introductory Approach. 4th Edition. Springer. 1984.
5. D. C. Lay : Linear Algebra and its Application. 3rd Edition. Pearson Education India.2009.
6. Seymour Lipschutz : Theory and Problems of Linear Algebra. SI (metric) edition. Schaum's outline series. McGraw Hill Publications. 1987.
7. K. Hoffman and R. Kunze :Linear Algebra. 2nd Edition. Prentice Hall India Ltd. 1978.
8. S. Lang :Linear Algebra. 3rd Edition . 11th Printing. Springer. 2004.
9. S. Kumaresan : Linear Algebra-A geometric approach. Prentice Hall India Private Limited. 2000.
10. D. S. Dummit and R. M. Foote. Abstract Algebra. Wiley. 2003.

QUESTION PAPER PATTERN

Code number: MT 7321

Title of the paper: LINEAR ALGEBRA

Paper Pattern: Students will have to answer 5 out of 7 main questions. Each main question will be worth a total of 10 marks.

The end semester question paper will have a weightage of 35% of the questions from the first half of the syllabus (the portions covered for the mid-semester examination) and a weightage of 65% of the questions from the second half of the syllabus (the portions not covered for the mid-semester examination).

Course Outcomes: At the end of the Course, the Student should

CO1	Have enhanced their knowledge of Linear Algebra by coming across a more general theory of Linear Algebra which is not restricted to finite dimensional vector spaces. Know more non-trivial examples of vector spaces and linear transformations and also know about vector spaces with some additional structures like inner product spaces, endomorphism rings of some fixed vector space etc.
CO2	Understand the crucial fact that to define a linear map, all one needs to do is to define any set theoretic map on a basis. Be able to understand the connection between algebra and geometry wherever possible.
CO3	Be able to apply the theorems learnt during the course for constructing algorithms for various computations.
CO4	Be able to analyze the given data and find ways for writing more efficient algorithms for computing the eigenvalues, for identifying the correct Jordan canonical form, for computing minimal polynomials etc.

Semester	**I**
Paper Code	**MT 7424**
Paper Title	**Ordinary Differential Equations**
Number of teaching hours per week	04
Total number of teaching hours per semester	60
Number of credits	04

Objective of the Paper:
To learn the basic techniques of solving ordinary differential equations and the stability of these solutions.

Syllabus:

Unit 1:
Introduction. Fundamental Theorem (Basic existence theorem). Example of ODE without solution. First order linear differential equations. Linear dependence. Wronskian. Abel's formula. Fundamental sets of solutions. Equations with constant coefficients. Method of Undetermined Coefficients. Non-homogeneous equations. Growth and Decay Phenomena. Mixing Phenomena. Spring problem.

(15 hours)

Unit 2:
A Review of Power Series. Series solutions. Solution at an ordinary point. Analyticity of solutions at an ordinary point. Regular singular points. Solution at a regular singular point. The method of Frobenius. The gamma function. Bessel's Equation.

(15 hours)

Unit 3:
Introduction to eigenvalue problems. The adjoint equation. Properties of self-adjoint problems. Sturm- Liovuelle's theorem. Characteristic Values and Characteristic Functions. Green's function. Self-Adjoint eigenvalue problems. Orthogonality of Characteristics function. Expansion of a function in a series of orthonormal functions. System of differential equations. Equilibrium points with example. First order systems. Systems with constant coefficients. Applications.

(15 hours)

Unit 4:
Nonlinear differential equations. First order differential equations. Exact solutions. Some special type of second order equations. Existence and uniqueness of solutions. The Phase Plane. Critical points. Stability for nonlinear systems (Liapunov). Perturbed linear systems.

(15 hours)

TEXT BOOKS:

1. S.L. Ross: Differential equations. John Wiley and Sons. New York. 3rd edition. 1984.
2. A. L. Rabenstein. An Introduction to Differential Equations. Academic Press. International Edition. 2014.

REFERENCE BOOKS:

1. A.C. King, J. Billingham and S.R. Otto. Differential equations. Cambridge University Press. 2006.
2. E.A. Coddington and N. Levinson. Theory of ordinary differential equations. McGraw Hill. 1955.
3. E.D. Rainville and P.E. Bedient. Elementary Differential Equations. McGraw Hill. New York. 1969.
4. G.F. Simmons. Differential Equations. Tata McGraw Hill Edition. New Delhi. 1974.
5. M.S.P. Eastham: Theory of ordinary differential equations. Van Nostrand. London. 1970.
6. S. J. Farlow. An Introduction to Differential Equations and their Applications. Dover Publications Inc. 2006.
7. Garrett Birkhoff and Gian-Carlo Rota. Ordinary Differential Equations. John Wiley and sons. 4th edition. 1991.

QUESTION PAPER PATTERN
Code number: MT 7424
Title of the paper: ORDINARY DIFFERENTIAL EQUATIONS
Paper Pattern: Students will have to answer 5 out of 7 main questions. Each main question will be worth a total of 10 marks.
The end semester question paper will have a weightage of 35% of the questions from the first half of the syllabus (the portions covered for the mid-semester examination) and a weightage of 65% of the questions from the second half of the syllabus (the portions not covered for the mid-semester examination).
Course Outcomes: At the end of the Course, the Student should

CO1	Recognize and classify ordinary differential equations. Define Ordinary and Singular points of Differential Equations. Identify various methods to solve different kinds of ODE.
CO2	Interpret the type of solution of an ODE (for eg. Power series solution.) Understand how to find other solutions of an ODE if one of the solutions is given. Classify the 2 nd Order differential equations based on their properties and orthogonality
CO3	Apply the techniques such as the power series method, Green's function method or Lyopunov method to solve problems.
CO4	Analyze solutions of third order Differential equations, zeroes of solutions, critical points and their stabilities, and interpret it on the Phase plane.

Semester	**I**
Paper Code	**MT 7524**
Paper Title	**Discrete Mathematics and Graph Theory**
Number of teaching hours per week	04
Total number of teaching hours per semester	60
Number of credits	04

Objectives:
To develop Mathematical maturity (i.e; the ability to understand and create mathematical arguments). To get an insight into how to utilize graph theoretical methods to analyse various connectivity patterns, data mining, image segmentation, clustering, image capturing and networking in the field of study and research.

Syllabus:

Unit 1:
Discrete Mathematics: Mathematical logic, Rules of inference, Recurrence relations, Modeling with recurrence relations with examples of Fibonacci numbers, Solving linear and non-linear recurrence relations, Generating Functions, Counting Problems and Generating Functions, Using Generating Functions to Solve Recurrence Relations Representing relations using matrices and digraphs, Closures of relations, Transitive closures, Warshall's Algorithm, Partial Orderings, Lexicographic Order, Hasse diagrams, Maximal and Minimal elements, Lattices. Latin Squares.

(15 hours)

Unit 2:
Fundamentals of graphs: Definition of graph, Applications of graphs, Finite and Infinite graphs, Incidence and degree, Isolated vertex, Pendent vertex and Null graph. Directed graph, Types of digraphs, Digraphs and Binary relations, Directed paths and connectedness, Euler digraphs.
Isomorphism, Subgraphs, A puzzle with multicolored cubes, Walks, Paths and Circuits, Connected graphs, disconnected graphs and components, Euler graphs, Operations on graphs, Hamiltonian paths and circuits, The traveling salesman problem.

(15 hours)

Unit 3:
Trees, Cut sets and Matrix representation of graphs: Trees, Some properties of trees, Pendent vertices in a tree, Distance and centers in a tree, Rooted and binary trees, On counting trees, Spanning trees, Fundamental Circuits, Finding all spanning trees of a graph, Spanning trees in a weighted graph. Cut sets, Some properties of a cut set, All cut sets in a graph, Fundamental circuits

and cut sets, Connectivity and separability. Incidence matrix, Circuit matrix, Fundamental circuit matrix, Cut set matrix, Path matrix, Adjacency matrix.

(15 hours)

Unit 4:

Coloring and Domination: Coloring, The Four color problem, Vertex coloring, Chromatic number, clique number, Edge coloring, Edge chromatic number, The five color theorem, Chromatic polynomial, Ramsey Theory.

Domination concepts: Open neighborhood, Closed neighborhood, Dominating sets in graphs, Minimum dominating sets, Domination number. Bounds of domination number in terms of size, order, degree, diameter. Minimal dominating sets, Total domination, Total domination number.

(15 hours)

TEXT BOOKS:

1. K. Rosen. Discrete Mathematics and its Applications. WCB McGraw-Hill. 8th edition. 2011.
2. J.H.Van Lint and R.M. Wilson. A course on combinatorics. Cambridge University Press. 2006.
3. N. Deo: Graph Theory: Prentice Hall of India Pvt. Ltd. New Delhi, 1990.
4. G. Chartrand and Ping Zhang: Introduction to Graph Theory. McGrawHill, International edition (2005)24.
5. D.B.West, Introduction to Graph Theory,Pearson Education Asia, 2nd Edition, 2002.

REFERENCE BOOKS:

1. F. Harary: Graph Theory, Addison -Wesley, 1969.
2. Charatrand and L. Lesnaik- Foster: Graph and Digraphs, CRC Press (Third Edition), 2010.
3. T.W. Haynes, S.T. Hedetniemi and P. J. Slater: Fundamental of domination in graphs, Marcel Dekker. Inc. New York.1998.
4. J. Gross and J. Yellen: Graph Theory and its application, CRC Press LLC, Boca Raton, Florida, 2000.
5. Norman Biggs: Algebraic Graph Theory, Cambridge University Press (2nd Ed.)1996.
6. Godsil and Royle: Algebraic Graph Theory: Springer Verlag, 2002.
7. J.A.Bondy and V.S.R.Murthy: Graph Theory with Applications, Macmillan, London, (2004).
8. J.P. Tremblay and R.P. Manohar . Discrete Mathematical Structures with applications to computer science. McGraw Hill. 1975.
9. H.J. Ryser. Combinatorial mathematics. American Mathematical Soc., 1963.
10. R.A. Beeler. How to Count: An Introduction to Combinatorics and Its Applications. Springer, 2015.

QUESTION PAPER PATTERN

Code number: MT 7524

Title of the paper: DISCRETE MATHEMATICS AND GRAPH THEORY

Paper Pattern: Students will have to answer 5 out of 7 main questions. Each main question will be worth a total of 10 marks.

The end semester question paper will have a weightage of 35% of the questions from the first half of the syllabus (the portions covered for the mid-semester examination) and a weightage of 65% of the questions from the second half of the syllabus (the portions not covered for the mid-semester examination).

Course Outcomes: At the end of the Course, the Student should

CO1	Have knowledge of discrete mathematics and graph theory techniques and ability to solve problems of computer science, networking and problems involved in different fields of study and research.
CO2	Understand problems of Engineering and physical sciences, express them in terms of graphs and use theoretical knowledge to get solutions.
CO3	Apply fundamental concepts, definitions, lemmas and theorems in the appropriate situations to establish results of their research work.
CO4	Analyse various practical problems of real life and use mathematical thinking to find the solution.
CO5	Evaluate and synthesize research articles which are published.
CO6	Create mathematical modeling for the purpose of simplified representation of reality, to mimic the relevant features of the system being analysed.

Semester	**I**
Paper Code	**MT 7P124**
Paper Title	**Linear Algebra and ODE with SageMath**
Number of teaching hours per week	04
Total number of teaching hours per semester	44
Number of credits	02

Objective of the paper:
To use SageMath, a Python based free and open source computer algebra system (CAS) to explore concepts in Applied Linear Algebra.

Syllabus:
Session 1: Introduction to SageMath. Special Matrix constructors (Circulant Matrices, Cauchy Matrix, Permutation Matrix, Vandermonde Matrices, Tridiagonal Matrices, Idempotent Matrices, Nilpotent Matrices, Permutation Matrices, Stochastic Matrices, Doubly Stochastic Matrix.). Matrices over Rings such as $\mathbb{Z}$, $\mathbb{Q}$, $\mathbb{R}$, $\mathbb{C}$, Finite Fields etc.
Session 2: Properties of special matrices.
Session 3: Eigenvalues and Eigenvectors. Bounds of Eigenvalues. Gershgorin Disc Theorem, Interlacing Lemma, Courant-Fischer, Weyl and Cauchy Theorems.
Session 4: Positive definite matrices.
Session 5: Linear Transformation, Visualization of Linear Transformation: Rotation, Reflection, Scaling as a Linear Transformation.
Session 6: Inner Product, Norm of Vectors. Polarization, parallelogram and Cauchy-Schwarz identities.
Session 7: Gram-Schmidt Orthogonalization and diagonalization.
Session 8: Matrix Decompositions: QR and Cholesky Factorization.
Session 9: Linear and nonlinear differential equations. Plotting analytic and numerical solutions.

Semester	**I**
Paper Code	**MT 7P224**
Paper Title	**Graph Theory with SageMath**
Number of teaching hours per week	04
Total number of teaching hours per semester	44
Number of credits	02

Objectives:
To use SageMath, a Python based free and open source computer algebra system (CAS) to explore concepts in Graph Theory.

Syllabus:
Session 1: Introduction to graphs in SageMath: Visualization - Plotting special graphs such as cycles, path, complete graph, Petersen graph. Graph parameters - order, size, vertex degrees, connectedness. Checking whether a graph is Eulerian, regular, degrees.
Session 2: Directed graphs: Digraphs, Creating and plotting digraphs, underlying graph of a digraph, connected digraph, weakly and strongly connected digraph, incidence matrix of a digraph, incidence matrix is unimodular, the order of the digraph is equal to the sum of rank of its incidence matrix and its number of components.
Session 3: Adjacency matrix: Adjacency matrix of an undirected graph, computing number of edges, number of triangles and number of k-walks of a graph using its adjacency matrix.
Session 4: Laplacian matrix: Laplacian matrix of a graph, relation between Laplacian matrix, distance matrix and adjacency matrix, Laplacian matrix as the product of incidence matrix and its transpose, laplacian matrix is positive semidefinite, computing rank of Laplacian matrix, row sum and column sum of laplacian matrix is zero, cofactors of any two elements of the Laplacian matrix are same.
Session 5: Trees 1: Creating and plotting trees, trees on n vertices has n-1 edges, a graph is a tree if and only if there exists a unique path between any two vertices, every tree has at least two leaves.
Session 6: Trees 2: Finding eccentricities, radius, diameter and the centers of a tree, a tree contains maximum two centers, if a tree has two centers then they are adjacent, computing length of a path for a tree using Laplacian matrix , distance matrix of a graph, distance matrix of a tree has one positive eigenvalue and n-1 negative eigenvalue, relation between eigenvalues of distance matrix and Laplacian matrix.
Session 7: Graph connectivity 1: Deletion of a vertex, deletion of a edge, cut vertex, cut edge, characterisation of cut vertices in graph, every edge in a tree is a bridge, adding an edge in a tree forms exactly one cycle, center of any tree remains unchanged after removal of leaves.
Session 8: Graph connectivity 2: Vertex connectivity, edge connectivity, relation between vertex

connectivity and edge connectivity, relation between number of spanning trees in a graph, the graph obtained by deleting and contracting an edge, Matrix-Tree theorem.

Session 9: Graph products: Cartesian product, lexicographic product, direct product, distance formula for cartesian product, distance formula for lexicographic product, distance formula for direct product.

Semester II

Semester	II
Paper Code	**MT 8121**
Paper Title	**Algebra-II**
Number of teaching hours per week	04
Total number of teaching hours per semester	60
Number of credits	04

Objective of the Paper:
The core objective of the paper is to learn the elegant "Fundamental Theorem of Galois Theory" and to prove that a general quintic doesn't possess any formula (which involves addition, subtraction, multiplication, division and taking nth roots) to find its roots.

Syllabus:

Unit 1:
Chapter 1: Basic Theory of Field Extensions: Characteristic of a field, Degree of an extension, Any polynomial f over a field F has a root in an extension K of F. Field generated by elements. Explicit description of K (basis of K as a vector space and understanding K as adjoining a root of an irreducible factor of f to F.
Chapter 2: Algebraic Extensions: Definition of Algebraic element and minimal polynomial of an algebraic element. Important theorems related to algebraic elements and minimal polynomials. Understanding quadratic extension over a field of characteristic not equal to 2. An extension is finite iff it is generated by finitely many algebraic elements. The property of an extension being algebraic is transitive.
Chapter 3: Splitting Field and Algebraic Closure: Definition of splitting field of a polynomial over a field and existence of splitting field. Computing splitting fields of different polynomials over specified fields . Introducing cyclotomic fields as splitting fields of $x^n - 1$. Primitive roots of unity. Uniqueness of splitting field. Definition of algebraic closure of a field and algebraically closed field. Existence of an algebraically closed field (without proof).

(20 hours)

Unit 2:
Chapter 4: Separable Extensions: Definition of separable polynomial over a field. Derivative of a polynomial and criterion for a polynomial to be separable. Examples of separable and inseparable polynomials. Understanding when an irreducible polynomial is separable. Existence and Uniqueness of finite fields.

Chapter 5: Cyclotomic Polynomials: Defining the nth Cyclotomic Polynomial and computing cyclotomic polynomials. Proving that the n^{th} cyclotomic polynomial is an irreducible monic polynomial of degree $\varphi(n)$ with integer coefficients.

(10 hours)

Unit 3:

Chapter 6: Automorphism group of a field extension: Computing the automorphism group of different extensions. Definition of Galois extension. Different examples and non-examples of Galois extension.

Chapter 7: Fundamental Theorem of Galois Theory: An extension is Galois if and only if it is the splitting field of a separable polynomial. Fundamental Theorem of Galois Theory. Applying the fundamental theorem to find all the intermediate fields of different extensions. Finite fields over its prime sub-field are Galois extensions.

(20 hours)

Unit 4:

Chapter 8: Insolvability of quintics: Cyclotomic Extensions, Abelian Extensions, Galois Group of Polynomials, Symmetric functions, Discriminant of a polynomial. Characterizing the Galois group of a polynomial through its discriminant. A general polynomial of degree more than 4 can not be solved by radicals.

(10 hours)

TEXT BOOKS:

1. D. S. Dummit and R. M. Foote. Abstract Algebra. Wiley. 2003.
2. J. A. Gallian. Contemporary Abstract Algebra. . 4th Edition. Narosa Publishing. 2011.

REFERENCE BOOKS:

1. I. N. Herstein. Topics in Algebra. 2nd Edition. Wiley. 1975.
2. I. S. Luthar and I. B. S. Passi. Algebra Volume-IV Field Theory. Narosa Publishing House. 2013.
3. J. B. Fraleigh. A first course in Abstract Algebra. 7th Edition Pearson Education India. 2002.
4. M. Artin . Algebra. 2nd Edition Pearson Education India. 2017.
5. S. Lang. Algebra. 3rd Edition. Springer. 2002.

QUESTION PAPER PATTERN

Code number: MT 8121

Title of the paper: ALGEBRA II

Paper Pattern: Students will have to answer 5 out of 7 main questions. Each main question will be worth a total of 10 marks.

The end semester question paper will have a weightage of 35% of the questions from the first half of the syllabus (the portions covered for the mid-semester examination) and a weightage of 65% of the questions from the second half of the syllabus (the portions not covered for the mid-semester examination).

Course Outcomes: At the end of the Course, the Student should

CO1	Have developed good knowledge of Splitting fields, Separable extensions, Finite Fields, Automorphism groups of an extension.
CO2	Understand the Fundamental Theorem of Galois Theory and insolvability of quintics.
CO3	Be able to apply the theory to compute splitting fields of different polynomials and automorphism groups of different extensions. Be able to apply Fundamental Theorem of Galois Theory to compute intermediate fields of any extension and its properties.
CO4	Be able to analyze which method of solution is the easiest to solve a given problem.
CO5	Be able to critique various proof methods for a particular theorem and explain why (or why not) one way is more useful than the other.
CO6	Be able to create examples and counterexamples of field extensions and the automorphism group of them.

Semester	**II**
Paper Code	**MT 8221**
Paper Title	**Measure and Integration**
Number of teaching hours per week	04
Total number of teaching hours per semester	60
Number of credits	04

Objective of the Paper:
To comprehend the basics of sigma algebras, measurable spaces and measurable functions. To understand the failings of the Riemann integral and learn how the Lebesgue integral is a generalization of Riemann integration.

Syllabus:

Unit 1:
Lebesgue Measure: Failure of the Riemann integral - sequences of integrable functions whose limit is not integrable, non-interchangeability of limit and integral sign, need of a general theory of integration, need of a generalization of the concept of area. Lebesgue outer measure on R^n and its properties. Sigma algebras. Measures on a sigma algebra. Properties of a measure and Borel Cantelli Lemma. Measurable sets. Lebegue measure on R^n. Properties of Lebesgue measure. Lebesgue sigma algebra. Non-measurable sets. Cantor set and sets of measure zero. Borel sets. Borel sigma algebra.

(15 hours)

Unit 2:
Measurable Functions: Measurable functions. Examples of measurable functions. Properties of measurable functions. Characteristic functions and simple functions. Approximating measurable functions by simple functions. Littlewood's three principles (includes Egorov's and Lusin's Theorems). .

(15 hours)

Unit 3:
Integration Theory: Lebesgue Integral of simple functions and its properties. Lebesgue integral of bounded measurable functions supported on sets of finite measure and its properties. Bounded convergence theorem. Lebesgue integral on [a,b] is the same as the Riemann integral. Lebesgue integral of non-negative measurable functions and its properties. Fatou's lemma and monotone convergence theorem. Lebesgue integral for any measurable function. Lebesgue (Dominated) convergence theorem. Invariance Properties of the integral. Fubini's Theorem (without proof) and

its consequences. Product measure.

(15 hours)

Unit 4:

Differentiation: Differentiation of Monotone functions. Vitali covering lemma. Functions of Bounded variation. Differentiability of an indefinite integral. Absolute continuity.

Lp spaces: L^1spaces and Riesz-Fischer Theorem in L^1. L^pspaces. Holder and Minkowski inequalities. Convergence and completeness. Bounded linear functionals. Ries-Fischer theorem in L^p. Riesz representation theorem and its consequences.

(15 hours)

TEXT BOOKS:

1. E.M Stein and R. Shakarchi, Real Analysis - Measure Theory, Integration and Hilbert Spaces. New age international publishers. 2010.
2. S. Kesavan, Measure and Integration. Hindustan Book Agency. 2019.

REFERENCE BOOKS:

1. P.R. Halmos, Measure Theory, East West Press, 1962.
2. W. Rudin, Real and Complex Analysis, McGraw Hill , 1966.
3. P. K. Jain, V. P. Gupta, P. Jain, Lebesgue Measure and Integration. Anshan Publications, 2nd edition. 2012.
4. M. M. Rao, Measure Theory and Integration. CRC press, 2nd edition. 2004.
5. F. Morgan, Geometric Measure Theory. Academic Press, 5th edition. 2016.
6. H.L. Royden, Real Analysis, Macmillan, 1963.

QUESTION PAPER PATTERN

Code number: MT 8221

Title of the paper: MEASURE AND INTEGRATION

Paper Pattern: Students will have to answer 5 out of 7 main questions. Each main question will be worth a total of 10 marks.

The end semester question paper will have a weightage of 35% of the questions from the first half of the syllabus (the portions covered for the mid-semester examination) and a weightage of 65% of the questions from the second half of the syllabus (the portions not covered for the mid-semester examination).

Course Outcomes: At the end of the Course, the Student should

CO1	Have developed good knowledge of the development of the Lebesgue integral. Know some of the failings of the Riemann theory and how Lebesgue theory compensates for them.
CO2	Understand the techniques involved in checking properties of measures, sigma algebras and measurable functions.
CO3	Be able to apply the theorems learnt in each topic to solve problems, particularly

	those involving the Littlewood’s three principles.
CO4	Be able to analyse which method of solution is the easiest to solve a given problem.
CO5	Be able to critique various proof methods for a particular theorem and explain why (or why not) one way is more useful than the other.

Semester	**II**
Paper Code	**MT 8325**
Paper Title	**Complex Analysis**
Number of teaching hours per week	04
Total number of teaching hours per semester	60
Number of credits	04

Objective of the Paper:
To comprehend the basics of Analytic function, its properties and its behavior in various domains. To get an understanding of some standard results related to the analytic function defined on the entire space and on a unit circle.

Syllabus:

Unit 1:
Analytic functions and the C-R equations. The Exponential, Sine and Cosine complex functions. Properties of Line integral. The closed curve theorem for Entire function. Cauchy Integral formula. Taylor series expansion of Entire function. Liouville Theorem. Fundamental Theorem of Algebra. Zeros of Analytic function. Jensen's formula. Gauss-Lucas Theorem.

(14 Hours)

Unit 2:
Power series representation for Analytic function. Uniqueness theorem. Mean Value theorem. Maximum Modulus theorem. Minimum Modulus theorem. Critical points and Saddle points. Open Mapping theorem. Schwarz Lemma. Morera's theorem.

(14 Hours)

Unit 3:
The General Cauchy Closed Curve theorem. Classification of Isolated singularities. Riemann Principle of Removable singularities. Casorati-Weierstrass Theorem. Laurent Expansion. Winding Numbers and Cauchy's Residue Theorem. Application of the Residue theorem. Argument principle. Rouche's Theorem. Hurwitz's Theorem.

(16 Hours)

Unit 4:
Evaluation of Definite Integral by Contour Integral Techniques. Application of Contour Integral Methods to Evaluation and Estimation of sums. Meromorphic functions. Conformal equivalence. Conformal Mapping. Riemann Mapping theorem. Harmonic functions. Mean-Value theorem for Harmonic Functions.

(16 Hours)

TEXTBOOKS:

1. J. Bak and D.J. Newman, Complex Analysis, Springer. 2010.
2. E. Stein and R. Shakarchi, Complex Analysis, New Age International Publishers, 2010.

REFERENCE BOOKS:

1. J. B. Conway. Functions of one complex variable. Narosa. 1987.
2. L.V. Ahlfors. Complex Analysis. McGraw Hill. 1986.
3. T. W. Gamelin. Complex Analysis. Springer-Verlag. 2006.
4. R. Nevanlinna. Analytic functions. Springer. 1970.
5. E. Hille. Analytic Theory. Volume I. Ginn. 1959.
6. M. J. Ablowitz, A. S. Fokas. Complex Variables: Introduction and Applications. Cambridge Texts in Applied Mathematics. 2003.
7. S. Ponnuswamy. Foundations of Complex Variables. Alpha Science. 2nd edition. 2011.

QUESTION PAPER PATTERN
Code number: MT 8325
Title of the paper: COMPLEX ANALYSIS
Paper Pattern: Students will have to answer 5 out of 7 main questions. Each main question will be worth a total of 10 marks.
The end semester question paper will have a weightage of 35% of the questions from the first half of the syllabus (the portions covered for the mid-semester examination) and a weightage of 65% of the questions from the second half of the syllabus (the portions not covered for the mid-semester examination).

Course Outcomes: At the end of the Course, the Student should

CO1	Have developed a good knowledge about Analytic functions, its properties and its behavior in various domains. Students have basic knowledge of some standard results relating to it.
CO2	Have understood geometrically the properties of the analytic functions. Students have understood the different techniques to check a given function is analytical. Students also have understood to methods to determine the zeros and residues of the analytic function
CO3	Students will be able to distinguish the methods to determine the zeros and residues of the analytic function and explain which methods are more suited
CO4	Students will be able to create different mappings between complex spaces.

Semester	II
Paper Code	**MT 8421**
Paper Title	**Partial Differential Equations**
Number of teaching hours per week	04
Total number of teaching hours per semester	60
Number of credits	04

Objective of the Paper:
To understand the basics of solving standard partial differential equations. Also, to learn various boundary value problems with their applications.

Syllabus:

Unit 1:
First Order Linear Partial Differential Equations: Origin of partial differential equations. Lagrange's equation Pp+Qq=R and problems based on each type. Integral surface passing through a given curve. Surfaces orthogonal to a given curve. Geometrical description of solutions of Pp+Qq=R.

(5 hours)

Unit 2:
Second Order Linear Partial Differential Equations:
Linear, Non-Linear and Quasi linear PDEs. Superposition principle. Classification of second-order linear partial differential equations into hyperbolic, parabolic and elliptic PDEs. Reduction of 2nd order linear PDEs to canonical forms and their general solution. Solution of linear Homogeneous and Non-Homogeneous PDEs with constant coefficients, PDEs reducible to constant coefficients, variable coefficients. Monge's method of Integration with distinct intermediate integral.

(20 hours)

Unit 3:
Heat, Wave and Laplace equations: Solution of heat, wave and Laplace equations by the method of separation of variables and integral transforms. Cauchy Problem (D'Alembert's and Riemann Volterra method). Duhamel's principle for wave and heat equation. Dirichlet, Neumann and Mixed problems in a rectangle for Laplace equation. Solution of heat, wave and Laplace equations in cylindrical and spherical polar coordinates.

(25 hours)

Unit 4:
Green's Function: Method of Eigenfunctions of expansion and method of Green's function

(Integral representation of the solution) for Heat equation, Wave equation and Laplace equation.

(10 hours)

TEXT BOOKS:

1. M. D. Raisinghania. Advanced differential equations. S.Chand. 19th edition. 2018.
2. K .S. Rao. Partial Differential Equations. PHI Learning Private limited. 3rd edition. 2013.

REFERENCE BOOKS:

1. V. Sundarapandian. Ordinary and Partial differential equations. McGraw Hill. 2012.
2. I. N. Sneddon. Elements of Partial Differential Equations. McGraw Hill Book company Inc. 2006.
3. M. G. Smith. Introduction to the theory of partial differential equation. Van Nostrand.1967.
4. F. Treves. Basic linear partial differential equations. Academic Press. 1975.
5. L. Debnath. Nonlinear PDEs for Scientists and Engineers. Birkhauser. Boston. 2007.
6. F. John. Partial differential equations. Springer. 1971.

QUESTION PAPER PATTERN

Code number: MT 8421

Title of the paper: PARTIAL DIFFERENTIAL EQUATIONS

Paper Pattern: Students will have to answer 5 out of 7 main questions. Each main question will be worth a total of 10 marks.

The end semester question paper will have a weightage of 35% of the questions from the first half of the syllabus (the portions covered for the mid-semester examination) and a weightage of 65% of the questions from the second half of the syllabus (the portions not covered for the mid-semester examination).

Course Outcomes: At the end of the Course, the Student should

CO1	Have developed knowledge of first and second order partial differential equations along with different methods employed to obtain the solution for the same. Solution of heat, wave and Laplace equations are found under various boundary conditions involved.
CO2	Be able to understand different methods that can be incorporated to solve the multivariable function subjected to various boundary conditions.
CO3	Be able to analyse qualitative properties involved in the solution of the problem and adopt a suitable method to find the solution.
CO4	Be able to evaluate the solution of the problem that involves multivariable functions. For instance, problems involving propagation of heat or sound, fluid flow, mass transfer, wave theory.
CO5	Be able to create equations that impose relations between various partial derivatives of a multivariable function.

Semester	**II**
Paper Code	**MT 8521**
Paper Title	**Topology**
Number of teaching hours per week	04
Total number of teaching hours per semester	60
Number of credits	04

Objective of the Paper:
To comprehend the basics of Riemann Integration, Sequences and Series of functions. To generalize the concept of distance in the real line and thus understand the notion of Metric Spaces.

Syllabus:
Unit 1:
Introduction to Topology: Definition and examples of topological spaces. Basis for a topology. Product Topology (finite product only). Subspace Topology. Neighborhoods and Limit points. Closed Sets and Limit points. Closure, Interior and Boundary of a set. Hausdorff Space.(Excluding the concept of finer and coarser, order topology, box topology).

(12 hours)

Unit 2:
Continuous Functions: Definition and examples of continuous function. Equivalent definitions of continuity. Homeomorphism and examples. Pasting lemma. Maps into Product Spaces.
Metric topology. Sequence Lemma.

(12 hours)

Unit 3:
Connectedness and Compactness: Definition and examples. Union of connected sets having a point in common is connected. Image of a connected space under a continuous map is connected. A cartesian product of connected space is connected. Path connected spaces. Example of a topological space which is connected but not path connected (topologist's sine curve). Components and path components. (Excluding the concept of local connectedness).
Definition and Examples of Compact Spaces. Closed subspace of a compact space is compact. Compact subspace of a Hausdorff space is closed. Image of a compact set is compact under a continuous map. Tube lemma. The product of finitely many compact spaces is compact. Compactness and "finite intersection property". Compact subsets of the real line. Lebesgue number lemma. Uniform continuity and compactness. Limit point and sequential compactness. (Excluding the concept of local compactness)

(24 hours)

Unit 4:

Countability and Separation Axioms: First countable and Second Countable topological space. Hausdorff Space. Regular Space. Normal Space. Necessary and Sufficient condition for Regular and Normal Spaces. Subspace of regular is regular and subspace of normal is normal. Urysohn's Lemma. Urysohn Metrization theorem. Tietze Extension Theorem (without proof). Tychnoff Theorem (without proof).

(12 hours)

TEXT BOOKS:

1. J. Munkres. Topology. Pearson Education India. 2nd Edition. 2007

REFERENCE BOOKS:

1. J L. Kelley. General Topology. Van Nostrand. Princeton. 1955
2. J. B. Conway. A course in point set topology. UTM Series. Springer. 2013
3. K. D. Joshi. Topology. New Age International Private limited. 1983
4. M. A. Armstrong. Basic Topology. Springer India .1983.
5. G. F. Simmons. Introduction to Topology and Modern Analysis. Tata McGraw-Hill Education. 1963.

QUESTION PAPER PATTERN

Code number: MT 8521

Title of the paper: TOPOLOGY

Paper Pattern: Students will have to answer 5 out of 7 main questions. Each main question will be worth a total of 10 marks.

The end semester question paper will have a weightage of 35% of the questions from the first half of the syllabus (the portions covered for the mid-semester examination) and a weightage of 65% of the questions from the second half of the syllabus (the portions not covered for the mid-semester examination).

Course Outcomes: At the end of the Course, the Student should

CO1	Develop knowledge in basics, crucial definitions and theorems in topology and develop the ability to understand new definitions.
CO2	Understand the basics of the field of topology, with emphasis on those aspects of the subject that are basic to higher mathematics.
CO3	Be able to apply different proof writing techniques and write their own proofs
CO4	Be able to analyze which technique is most useful in demonstrating a particular property of a topological space.
CO5	Be able to critique various proof methods for a particular theorem and explain why (or why not) one way is more useful than the other.
CO6	Be able to create examples and counter-examples particularly when working with the questions on homeomorphisms, connected and compact spaces.

Semester	**II**
Paper Code	**MT 8624**
Paper Title	**Probability and Statistics**
Number of teaching hours per week	04
Total number of teaching hours per semester	60
Number of credits	04

Objective of the Paper:

This course aims to provide students with the foundations of probabilistic and statistical analysis mostly used in varied applications. It will also focus on the random variable, different types of distributions, sampling theory, to design a statistical hypothesis about the real world problem and to conduct appropriate tests for drawing valid inference about the population characteristics.

Syllabus:

Unit 1:

Data Presentation: diagrammatic and graphical methods. Exploratory Data Analysis using descriptive measures and graphical tools. Univariate Analysis: Measures of central tendency, positional averages, measures of dispersion, moments, skewness and kurtosis – Definition, properties and problems related to it.

Probability theory: random experiment, simple events, sample space - types of events, probability of an event, rules of probability, conditional probability, Bayes' theorem.

(15 hours)

Unit 2:

Probability distributions: random variables - discrete and continuous type, probability distribution table, Probability Mass Function and Probability Density Function Bernoulli, Binomial, Poisson, Geometric, Uniform, Exponential, Gamma and normal distributions - applications.

Joint distributions: Marginal and conditional distributions.

Markov chains with finite and countable state space, classification of states, limiting behaviour of n-step transition probabilities, stationary distribution.

(15 hours)

Unit 3:

Sampling methods - population and sample, parameter and statistic, concept of a random sample, simple random sampling, stratified sampling, systematic sampling, sample size determination.

Testing of hypothesis: null hypothesis, alternate hypothesis, test statistic, level of significance, p-value. Testing hypotheses about population mean, tests for proportions, tests concerning variance. Contingency tables, chi-square test for independence of attributes.

Correlation: Scatterplot, correlation coefficient and its properties, rank correlation, Test for correlation coefficient.
Regression: linear relationship, linear regression model, simple linear regression, Test for regression coefficients.

(20 hours)

Unit 4:
Analysis of variance: Completely randomized designs, randomized block designs and Latin-square designs.

(10 hours)

TEXT BOOKS:

1. Vinay K. Rohatgi and A. K. MD. Ehsanes Saleh, "An Introduction to Probability and Statistics", Wiley-Inter-science Publication, John Wiley and Sons, Inc, New York, Second Edition, 2001.
2. Johnson, R.A., Miller, I and Freund J., "Miller and Freund's Probability and Statistics for Engineers", Pearson Education, Asia, 8th Edition, 2015.

REFERENCE BOOKS:

1. S. C. Gupta, V. K. Kapoor. Fundamentals of Mathematical Statistics. Sultan Chand and Sons. 1st Edition. 2020.
2. Walpole. R.E., Myers. R.H., Myers. S.L. and Ye. K., "Probability and Statistics for Engineers and Scientists", 9th Edition, Pearson Education, Asia, 2010.
3. Devore. J.L., "Probability and Statistics for Engineering and the Sciences", Cengage Learning, New Delhi, 8th Edition, 2014.

QUESTION PAPER PATTERN
Code number: MT 8624
Title of the paper: PROBABILITY AND STATISTICS
Paper Pattern: Students will have to answer 5 out of 7 main questions. Each main question will be worth a total of 10 marks.
The end semester question paper will have a weightage of 35% of the questions from the first half of the syllabus (the portions covered for the mid-semester examination) and a weightage of 65% of the questions from the second half of the syllabus (the portions not covered for the mid-semester examination).

Course Outcomes: At the end of the Course, the Student should

CO1	Identify the types of data, use appropriate statistical terms to describe data and apply appropriate statistical methods to collect, organize, display, and analyze relevant data.

CO2	Define, explain the different statistical distributions, apply them to solve problems to find probabilities and predict the probability of certain events.
CO3	Apply the concepts of hypothesis testing using appropriate test static and make valuable conclusions by proper evaluation.
CO4	Analyze the different mathematical models with the help of statistical design and appropriate data, solve using appropriate methods and give inferences.

Semester	**II**
Paper Code	**MT 8P24**
Paper Title	**Probability and statistics with R Programming**
Number of teaching hours per week	04
Total number of teaching hours per semester	44
Number of credits	02

Objective of the paper:
To supplement the masters course with a basic knowledge of probability and statistics. To enable proficiency in R programming.

Syllabus:
Session 1: Basics of R programming and Diagrammatic Representation of Data:
Histogram, Frequency polygon, Dot Plots, Box Plot, Ternary Plot, Pie Chart, Bar Diagram.
Session 2: Univariate Analysis:
Measures of central tendency, positional averages, measures of dispersion.
Session 3: Central Moments, skewness and kurtosis with diagrammatic representations.
Session 4: Probability Distributions I:
Fitting of Data using Binomial, Poisson and Geometric distribution.
Session 5: Probability Distributions II:
Fitting of Data using Uniform, Exponential and Normal Distribution.
Session 6: Markov Process
Problems involving 1- step, 2-step Transition probabilities and Poisson birth and death processes.
Session 7: Parametric Testing of Hypothesis - I.
Problems on Test Concerning Population Mean and Proportions for large samples.
Session 8: Parametric Testing of Hypothesis - II.
Problems on Test Concerning Population Mean for small sample and test Concerning Variances.
Session 9: Bi-Variate Data Analysis:
Problems on Computation of Correlation Coefficient (Karl Pearson's and Spearman's Coefficient of Correlation) and Simple Linear Regression.
Session 10: ANOVA
Problems on Latin square design

Semester III

Semester	III
Paper Code	**MT 9122**
Paper Title	**Functional Analysis**
Number of teaching hours per week	04
Total number of teaching hours per semester	60
Number of credits	04

Objective of the Paper:

To learn the concept Norms, Normed Linear Spaces, Inner Product Spaces, Banach and Hilbert Spaces, their examples and properties.

Syllabus:

Unit 1 (Norm linear space and Banach space)

Definition and Examples of Normed Linear Spaces, Examples of norm linear space: Finite Dimensional spaces, spaces of sequences, spaces of measurable functions, inner product spaces. Definition and example of Banach spaces, Equivalence of norms, Any norm on a finite dimensional space is equivalent. Every finite dimensional space is Banach with respect to any norm. Riesz Lemma and Heine-Borel Theorem, A Banach space cannot have a denumerable basis.

20 hours

Unit 2 (Bounded operators)

Bounded operators on normed linear spaces: Bounded operators definition and equivalent conditions, Examples of bounded operator: Finite and Infinite matrix as bounded operator, orthogonal projection, Fredholm integral operator . Finding norms of bounded operators, $B(X, Y)$, the space of bounded linear maps between normed linear spaces. Completeness of $B(X, Y)$.

10 hours

Unit 3 (Geometry of Hilbert Spaces)

Hilbert Spaces, Orthonormal set and Orthonormal basis. Bessel's inequality, Fourier expansion and Parseval's formula , Riesz-Fischer theorem. Best approximation theorem and projection theorem. Riesz representation theorem.

15 hours

Unit 4

Hahn-Banach extension theorem and its consequences, Criterion for uniqueness of Hahn-Banach extension, Reflexive spaces, Minkowski functional, Hahn-Banach separation theorem and its consequences, Closed Graph theorem and its consequences, Principle of uniform boundedness, Open Mapping theorem.

15 hours

TEXTBOOKS:

1. M. T. Nair, Functional Analysis a first course, PHI, 2014.

2. B. V. Limaye, Functional Analysis, Wiley Eastern, 2014.
3. S. Kesavan, Functional Analysis, Hindustan Book Agency (TRIM), 2009.

REFERENCE BOOKS:

1. G. F. Simmons, Introduction to Topology and Modern Analysis, McGraw-Hill International Edition, 1963.
2. G. Backman and L. Narici, Functional Analysis, Academic, 1968.
3. P.R. Halmos, Finite dimensional vector spaces ,Van Nostrand, 1958.
4. E. Kreyszig, Introduction to Functional Analysis with Applications, John Wiley and Sons, 1978.

QUESTION PAPER PATTERN:

Code number: MT 9122

Title of the paper: Functional Analysis

Paper Pattern: Students will have to answer 5 out of 7 main questions. Each main question will be worth a total of 10 marks.

The end semester question paper will have a weightage of 35% of the questions from the first half of the syllabus (the portions covered for the mid-semester examination) and a weightage of 65% of the questions from the second half of the syllabus (the portions not covered for the mid-semester examination).

Course Outcomes: At the end of the Course, the Student should

CO1	Have a good knowledge of normed linear spaces, inner product spaces, Banach and Hilbert Spaces. Know various examples and properties of these spaces
CO2	Understand the geometry of inner products and norms
CO3	Be able to apply theorems learnt in each topic to solve problems
CO4	Be able to analyze which method of solution is the easiest to solve a given problem

Semester	**III**
Paper Code	**MT 9225**
Paper Title	**Classical and Continuum Mechanics**
Number of teaching hours per week	04
Total number of teaching hours per semester	60
Number of credits	04

Objective of the Paper:
To learn the fundamental concepts of solid and continuum mechanics and the conservation laws associated with them.

Syllabus:
Unit 1:
Classical Mechanics I: Coordinate systems. Plane polar, cylindrical and spherical polar co-ordinate systems. Frame of reference. Motion of system of particles. Degree of freedom and constraints. Generalized coordinates, Lagrangian form of D'Alembert's principle, generalized force, work with potential and kinetic energy, conservation of energy and Konig's theorem. Angular momentum of a system of particles and generalized momentum.

15 hours

Unit 2:
Classical Mechanics II: Lagrange's equation, Lagrange's equation of motion for holonomic and non-holonomic systems, Integrals of motion, ignorable coordinate, Routhian function, conservative system, Natural and Orthogonal system, Liouville's system. Equation of motion for small oscillations. Hamilton's equation, Hamilton's principle, forms of Hamilton's function, Principle of least action.

15 hours

Unit 3:
Continuum Hypothesis: Suffix notation. Comma notation. Gradient of a scalar, Divergence and Curl of a tensor. Configuration of a continuum. Mass and density. Description of motion in material and spatial coordinates. Deformation gradient tensor, deformation of a surface element and deformation of a volume element. Strain, Green's strain tensor, displacement, infinitesimal strain and rotation, compatibility condition. Motion, vorticity, path lines, stream lines, field lines and vertex lines. Reynold's transport formula and Kelvin's circulation theorem.

20 hours

Unit 4:
Fundamental Laws of Continuum Mechanics: Law of conservation of mass, equation of continuity in material form, conservation of linear momentum, equation of linear momentum in material form, balance of energy and equation of energy in material form.

10 hours

TEXT BOOKS:

1. D S Chandrashekharaiah and Lokenath Debnath, Continuum Mechanics, Elsevier Science, 2014.
2. H. Goldstein, Classical Mechanics, Narosa Publishing Home, New Delhi, 2001.
3. J. Marion and S. Thorntron, Classical Dynamics of Particles and Systems, Third Edition, Horoloma Book Jovanovich College Publisher, 2012.
4. P. V. Panat, Classical Mechanics, Narosa Publishing Home, New Delhi, 2013.

REFERENCE BOOKS:

1. N. C. Rana and P. S. Joag, Classical Mechanics, Tata Mc-Graw Hill Publishing Company Limited, New Delhi, 2015.
2. R. G. Takawale and P.S.Puranik, Introduction to Classical Mechanics, Tata Mc-Graw Hill Publishing Company Limited, New Delhi, 2008.
3. C.S. Jog, Continuum Mechanics Foundations and Applications of Mechanics, Cambridge-IISc Press, 3rd edition, Volume I. 2015.
4. George E Mase, Schaum's Outline of Continuum Mechanics, First edition, McGraw Hill, 2020.

QUESTION PAPER PATTERN
Code number: MT 9225
Title of the paper: Classical and Continuum Mechanics
Paper Pattern: Students will have to answer 5 out of 7 main questions. Each main question will be worth a total of 10 marks.
The end semester question paper will have a weightage of 35% of the questions from the first half of the syllabus (the portions covered for the mid-semester examination) and a weightage of 65% of the questions from the second half of the syllabus (the portions not covered for the mid-semester examination).

Course Outcomes: At the end of the Course, the Student should

CO1	The students undergoing this course acquire the ability to understand both Solid and Continuum mechanics, later they can specialize in any one of them.
CO2	Completion of this course will enable students to: convert from one co-ordinate to another coordinate system, determine the positions and velocity of an objects in different frame, differentiate between Lagrangian and Hamiltonian equation of motion, apply the tensor formalism, treat general stresses and deformations in continuous materials, formulate and solve specific technical problems of displacement, strain and stress and so on.
CO3	Model the system using conservation laws.
CO4	Help to choose a relevant paper in the following semester.

Semester	**III**
Paper Code	**MTDE 9322**
Paper Title	**Graphs and Matrices**
Number of teaching hours per week	04
Total number of teaching hours per semester	60
Number of credits	04

Objective of the Paper:
To learn the links between linear algebra and graph theory and apply linear algebraic techniques to derive properties of graphs.

Syllabus:

Unit 1:
Incidence Matrix of a directed graph. Rank and minors of the incidence matrix and its relation to connected components of a graph. Path matrix. Moore-Penrose inverse of incidence matrix. 0-1 incidence matrix. Adjacency Matrix. Eigenvalues of some graphs. Bounds on eigenvalues. Energy of a graph and its applications in chemistry.

20 hours

Unit 2:
Laplacian Matrix. Basic properties. Computing Laplacian eigenvalues. Bounds for Laplacian spectral radius. Edge-Laplacian of a tree. Signless Laplacian matrix.

10 hours

Unit 3:
Regular graphs. Perron-Frobenius Theory. Adjacency algebra of a regular graph. Complement and line graph of a regular graph. Algebraic Connectivity. Fiedler vector. Classification of trees. Characteristic edge and vertex of a tree.

15 hours

Unit 4:
Distance matrix of a graph. Distance matrix and Laplacian of a tree. Eigenvalues of the distance matrix of a tree. Resistance Distance Matrix. Network flows. Random walks on graphs. Effective resistance in electrical networks.

15 hours

TEXT BOOKS:

1. R B Bapat, Graphs and Matrices, Second Edition, Hindustan Book Agency, 2018.
2. Sebastian M Cioaba and M Ram Murty, A First Course in Graph Theory and Combinatorics, Hindustan Book Agency, 2009.

REFERENCE BOOKS:

1. D M Cvetkovic, M Doob and H Sachs, Spectra of Graphs, Theory and Applications, Third Edition,

Johann Ambrosius Bath, Heidelberg, 1995.
2. C Godsil and G Royle, Algebraic Graph Theory, Graduate Texts in Mathematics, 207, Springer-Verlag, New York, 2001.
3. N Biggs, Algebraic Graph Theory, Second Edition, Cambridge University Press, Cambridge, 1993.

QUESTION PAPER PATTERN
Code number: MTDE 9322
Title of the paper: Graphs and Matrices
Paper Pattern: Students will have to answer 5 out of 7 main questions. Each main question will be worth a total of 10 marks.
The end semester question paper will have a weightage of 35% of the questions from the first half of the syllabus (the portions covered for the mid-semester examination) and a weightage of 65% of the questions from the second half of the syllabus (the portions not covered for the mid-semester examination).

Course Outcomes: At the end of the Course, the Student should

CO1	Know some of the various matrices associated with graphs and their properties.
CO2	Understand the correlation between linear algebraic properties and graph theoretic properties.
CO3	Analyze the eigenvalue bounds and properties to determine whether a graph is connected, regular etc.
CO4	Apply the results learnt to latest research work in spectral graph theory

Semester	**III**
Paper Code	**MTDE 9425**
Paper Title	**Optimization Techniques**
Number of teaching hours per week	04
Total number of teaching hours per semester	60
Number of credits	04

Objective of the Paper:
To learn the various techniques involved in obtaining the optimum outcome to a given real life situation for the benefit of the people involved.

Syllabus:

Unit 1:
Linear programming problems. Model formulation and graphical solution. Various types of solutions. Simplex method of solving linear programming. Artificial variable techniques. Big M method. Principle of duality.

15 hours

Unit 2:
Transportation problem. Initial Basic Feasible Solution. North-West Corner Rule. Vogel's Approximation Method. MODI method of finding optimal solutions. Assignment problem. Sequencing problem. 'n jobs two machines' problem. 'n jobs m machines' problem. Replacement problem. Replacement of policy when the value of money changes/does not change with time. Replacement of equipment that fails suddenly.

15 hours

Unit 3:
Game theory. Two person zero sum games. Pure and Mixed strategies. Games with a saddle point. Principle of dominance. Graphical method. Decision analysis. Components of decision making. Decision making without probabilities. Maximin–minimax regret. Hurwicz and equal likelihood criterion. Decision making with probabilities. Expected value. Expected opportunity loss criterion.

15 hours

Unit 4:
Network flow models: Shortest route problem. Minimal Spanning Tree Problem. Maximal Flow Problem. DIJKSTRA'S ALGORITHM. The CPM and PERT Networks.

15 hours

TEXT BOOKS:

1. Hamdy A. Taha, Operations Research , An Introduction, 10th Edition, Prentice Hall of India Private Ltd, 2017.
2. Sharma J.K, Operations Research Theory and applications, Macmillan, 1997.

REFERENCE BOOKS:

1. Hillier F S and Lieberman, GJ. Introduction to Operations Research, 7th Edition, McGraw Hill, 2002.
2. Kanti Swarup, Manmohan and Gupta PK, Operations Research, Sultan Chand and Sons, New Delhi, 1985.

QUESTION PAPER PATTERN
Code number: MTDE 9425
Title of the paper: Optimization Techniques
Paper Pattern: Students will have to answer 5 out of 7 main questions. Each main question will be worth a total of 10 marks.
The end semester question paper will have a weightage of 35% of the questions from the first half of the syllabus (the portions covered for the mid-semester examination) and a weightage of 65% of the questions from the second half of the syllabus (the portions not covered for the mid-semester examination).

Course Outcomes: At the end of the Course, the Student should

CO1	The students will be able to access the situation in industry as to what shall be the next step in process
CO2	The students will learn how to make right decisions in pressure situations.
CO3	Students will be equipped to understand the various optimisation models in businesses
CO4	Students will be equipped to plan projects for organizations.

Semester	**III**
Paper Code	**MT 9525**
Paper Title	**Mathematical Methods**
Number of teaching hours per week	03
Total number of teaching hours per semester	45
Number of credits	03

Objective of the Paper:
Make the students acquire the knowledge of fundamental principles, methods and a clear perception of mathematical ideas and tools to interpret and solve problems in physical sciences and Engineering.

Syllabus:

Unit 1: Integral Equations

Definition of Volterra and Fredholm integral equations. Solution of Fredholm and Volterra's integral equations by the method of separable kernel, Neumann's series, Picard's method, iterated kernels, Symmetric kernel, Resolvent kernel method, Laplace transform method. Convergence for Fredholm and Volterra types. Reduction of initial value problems to Volterra integral equations, Transforming boundary value problems into Fredholm integral equations, Solving Eigenvalue problems of integral equations.

15 hours

Unit 2: Fourier Transforms

Fourier Integral theorem, Properties of Fourier Transform, Inverse Fourier Transform, Fourier cosine and Fourier sine transforms, Inverse Fourier cosine and sine transforms, Convolution Theorem, Solving integral equations using Fourier transform, Fourier Transform of the derivatives of functions, Parseval's Identity and problems, Application of Fourier transforms to the solution of initial and boundary value problems.

15 hours

Unit 3: Perturbation Theory and Asymptotic expansions

Elementary introduction, Application to polynomial equations and initial value problems for differential equations, Regular and singular perturbation theory, classification of perturbation problems as regular or singular, Asymptotic matching, Matched asymptotic expansions. Asymptotic expansion of functions. Power series as asymptotic series. Asymptotic forms for large and small variables. Asymptotic expansions of integrals. Method of integration by parts (include examples where the method fails). Laplace's method, Watson's lemma and problems.

15 hours

TEXT BOOKS:

1. C. M. Bender and S. A. Orszag, Advanced mathematical methods for scientists and Engineers (McGraw Hill, New York), 1978.

2. Brian Davies, Integral transforms and their Applications, Springer. 2002.

REFERENCE BOOKS:

1. R. P. Kanwal, Linear integral equations theory and techniques , Academic Press, New York, 1971.
2. Shanti Swarup, Integral equations , Krishna Prakashan Media (P) Limited, 1974.
3. I. N. Sneddon, Use of Integral Transforms, Tata-McGraw Hill, 1974.
4. R. Bracemell, Fourier Transform and its Applications, MacDraw hill, 1986.
5. L. Andrews and B. Shivamogg, Integral Transforms for Engineers, Prentice Hall of India, 2003.
6. J. K. Goyal and K. P. Gupta, Integral Transforms (Pragati Prakashan), 2007.

QUESTION PAPER PATTERN
Code number: MT 9525
Title of the paper: Mathematical Methods
Paper Pattern: Students will have to answer 5 out of 7 main questions. Each main question will be worth a total of 10 marks.
The end semester question paper will have a weightage of 35% of the questions from the first half of the syllabus (the portions covered for the mid-semester examination) and a weightage of 65% of the questions from the second half of the syllabus (the portions not covered for the mid-semester examination).

Course Outcomes: At the end of the Course, the Student should

CO1	Recognize and solve integral equations using various methods and reduce IVPs, BVPs and eigenvalue problems to integral equations.
CO2	Gain the knowledge of construction of Fourier transform and its applications.
CO3	Be able to derive and analyze properties of transforms which helps to study the applications of it in various fields.
CO4	Be able to apply Fourier transforms as a tool to get the solution of initial and boundary value problems.
CO5	Be able to calculate the ground state and excited state energies of various real life systems by using perturbation methods.
CO6	Understand Asymptotic expansion of functions, Power series as asymptotic series. Asymptotic forms for large and small variables.

Semester	**III**
Paper Code	**MT 9625**
Paper Title	**Numerical Analysis**
Number of teaching hours per week	04
Total number of teaching hours per semester	60
Number of credits	04

Objective of the Paper:
To enable students to understand the applications of iterative techniques, explicit and implicit techniques, analyze the techniques involved in constructing approximate polynomials, determine the intermediate values and implement the finite element method efficiently in order to solve a particular equation.

Syllabus:

Unit 1:
Interpolation and Numerical Linear Algebra.
Interpolation with unevenly spaced points: Lagrange's interpolation, Hermite's interpolation, Error Analysis, Cubic Spline interpolation.
LU Decomposition of Matrix, vector and matrix norms, Solution of Linear system - Gauss Elimination, Necessity of pivoting, Number of arithmetic operations, LU decomposition methods - Crout's and Cholesky decomposition, Solution of Tridiagonal systems, Ill conditioned linear system, Method for Ill conditioned systems.

15 hours

Unit 2:
Numerical Differentiation and Integration
Numerical Differentiation: Errors in Numerical Differentiation, Cubic Splines method, Differentiation formulae with function values. Derivative using Newton's Forward and Backward difference interpolation.
Numerical integration: Romberg's Method, Gaussian Integration, Two point and three-point Gaussian quadrature formulae, Evaluation of double integrals by Trapezoidal and Simpson's 1/3 rules, Error in Numerical Integration formula.

15 hours

Unit 3:
Numerical Solutions to Ordinary Differential Equations
Picard's method, Runge-Kutta methods for simultaneous first and second order equations, Predictor - Corrector methods: Milne's method, Adam-Bashforth method, Error analysis.
Boundary Value Problems: Finite difference methods, Shooting methods.

15 hours

Unit 4:
Numerical Solutions to Partial Differential Equations
Finite difference to partial derivatives: Laplace's and Poisson's equations on rectangular domain, One

dimensional heat flow equation by explicit (Schmidt method) and implicit (Crank Nicholson method) methods , One dimensional wave equation by explicit method.

15 hours

TEXT BOOKS:

1. S. S. Sastry, Introductory Methods of Numerical Analysis, Fifth Edition, PHI Learning Private Ltd., 2017.
2. Steven C. Chapra and Raymond P. Canale, Numerical Methods for Engineers, Seventh Edition, McGraw Hill Education Pvt Ltd, 2016.
3. S D Conte and Carl de Boor, Elementary Numerical Analysis: An algorithmic approach, Society for Industrial & Applied Mathematics,U.S, 2017.

REFERENCE BOOKS:

1. P.D.Sivaramakrishna and C.Vijayakumari, A Textbook of Numerical Methods, Pearson publications, 2013.
2. Brian Bradie, A Friendly Introduction to Numerical Analysis, Pearson Education, Asia, New Delhi, 2007.
3. C. F. Gerald and P. O. Wheatley, Applied Numerical Analysis, Pearson Education, Asia, 6th Edition, New Delhi, 2006.
4. K. Sankara Rao, Numerical Methods for Scientists and Engineers, Prentice Hall of India Pvt. Ltd, 3rd Edition, New Delhi, 2007.
5. Richard L. Burden and J. Douglas Faires, Numerical Analysis, Fourth Edition, P.W.S. Kent Publishing Company, 2007.

QUESTION PAPER PATTERN

Code number: MT 9625

Title of the paper: Numerical Analysis

Paper Pattern: Students will have to answer 5 out of 7 main questions. Each main question will be worth a total of 10 marks.

The end semester question paper will have a weightage of 35% of the questions from the first half of the syllabus (the portions covered for the mid-semester examination) and a weightage of 65% of the questions from the second half of the syllabus (the portions not covered for the mid-semester examination).

Course Outcomes: At the end of the Course, the Student should

CO1	Apply numerical methods to obtain approximate solutions to mathematical problems
CO2	Derive numerical methods for various mathematical operations and tasks, such as interpolation, differentiation, integration
CO3	Analyze and evaluate the accuracy of common numerical methods
CO4	Apply the knowledge of numerical methods and Solve first order ordinary differential equations

Semester	**III**
Paper Code	**MT 9P25**
Paper Title	**Numerical Analysis with SageMath**
Number of teaching hours per week	04
Total number of teaching hours per semester	48
Number of credits	02

Objective of the Paper:
To enable students to understand the applications of iterative techniques, explicit and implicit techniques, analyze the techniques involved in constructing approximate polynomials, determine the intermediate values and implement the finite element method efficiently in order to solve a particular equation.

Syllabus:

Session 1: Interpolation with unevenly spaced points I: Lagrange's interpolation, Hermite's interpolation.
Session 2: Interpolation with unevenly spaced points II: Cubic Spline interpolation.
Session 3: LU decomposition methods - Crout's and Cholesky decomposition, Solution of Tridiagonal systems
Session 4: Numerical Differentiation: Cubic Splines method, Differentiation formulae with function values. Derivative using Newton's Forward and Backward difference interpolation.
Session 5: Numerical integration: Evaluation of double integrals by Trapezoidal and Simpson's 1/3 rules.
Session 6: Picard's method, Runge-Kutta methods for simultaneous first and second order equations.
Session 7: Predictor - Corrector methods: Milne's method, Adam-Bashforth method.
Session 8: One dimensional heat flow equation by explicit (Schmidt method) and implicit (Crank Nicholson method) methods.
Session 9: Galerkian method.

Semester	**III**
Paper Code	**MT 9R125**
Paper Title	**Introduction to Mathematical Research**
Number of teaching hours per week	03
Total number of teaching hours per semester	33
Number of credits	02

Objective of the Paper:
To introduce students to research in Mathematics through hands-on training.

Syllabus:
Introduction to research and research methodology. Scientific methods. Choice of research problem. Literature survey and statement of research problem. Reporting of results. Roles and responsibilities of research student and guide.
Introducing Mathematical Journals. Reading a Journal article. Mathematics writing skills. Learning to type with LaTeX software.
The student will begin the study of a research paper(s) and will make presentations/working seminars to the supervisor(s). A project proposal will be the final presentation.

METHOD OF EVALUATION
Code number: MT 9R125
Title of the paper: Introduction to Mathematical Research

Course Code: MT9R25							
Survey of past years proposals	Weekly reports (average)	Knowledge of Journals	Learning Latex	First draft of research proposal	Final draft of research proposal	Research proposal presentation	Total marks (scaled to 50)
10	10	10	15	10	10	5	50

Course Outcomes: At the end of the Course, the Student should

CO1	Be able to search for and organize literature in a given research topic
CO2	Be able to use LaTeX software to create reports and beamer presentations
CO3	Be able to analyze which papers are relevant to current research in a topic
CO4	Be able to write a research proposal

Semester IV

Semester	**IV**
Paper Code	**MT 0125**
Paper Title	**Differential Geometry**
Number of teaching hours per week	04
Total number of teaching hours per semester	60
Number of credits	04

Objective of the Paper:
To equip the students with techniques that help in guessing the shapes of curves and surfaces in the usual Euclidean three dimensional space using basic calculus.

Syllabus:

Unit 1:
Calculus on Euclidean Space: Euclidean space. Natural coordinate functions. Differentiable functions. Tangent vectors and tangent spaces. Vector fields. Directional derivatives and their properties. 1-forms and problems pertaining to 1-forms.

6 hours

Unit 2:
Curves in E3. Velocity and speed of a curve. Reparametrization of a curve. Frame Fields: Arc length parametrization of curves. Vector field along a curve. Tangent vector field, Normal vector field and Binormal vector field. Curvature and torsion of a curve. The Frenet formulas. Properties of plane curves and spherical curves. Arbitrary speed curves. Cylindrical helix. Mappings of Euclidean spaces. Derivative map. Isometries of E3- Translation, Rotation and Orthogonal transformation. The derivative map of an isometry. Orientation. Euclidean Geometry. Congruence of Curves.

24 hours

Unit 3:
Calculus on a Surface: Coordinate patch. Monge patch. Surface in E3 . Special surfaces- sphere, cylinder and surface of revolution. Parameter curves, velocity vectors of parameter curves, Patch computation. Parametrization of surfaces - cylinder, surface of revolution and torus. Tangent vectors, vector fields and curves on a surface in E3. Directional derivative of a function on a surface of E3.

12 hours

Unit 4:
Covariant derivatives. Shape Operators: Definition of shape operator. Shape operators of sphere, plane, cylinder and saddle surface. Normal curvature, Normal section. Principal curvature and principal direction. Umbilic points of a surface in E3. Euler's formula for normal curvature of a surface in E3. Gaussian curvature, Mean curvature and Computational techniques for these curvatures. Minimal surfaces. Special

curves in a surface of E3 -Principal curve, geodesic curve and asymptotic curves. Special surface - Surface of revolution.

18 hours

TEXT BOOKS:

1. Barrett O' Neil, Elementary Differential Geometry, Academic Press, New York and London, 1966.
2. T. J. Willmore, An introduction to Differential Geometry, Clarendon Press, Oxford 1959**.**

REFERENCE BOOKS:

1. D. J. Struik, Lectures on Classical Differential Geometry, Addison Wesley, Reading, Massachusetts, 1961.
2. Nirmala Prakash, Differential Geometry- An integrated approach. Tata McGraw-Hill, New Delhi, 1981.
3. A. N. Pressley. Elementary Differential Geometry. Springer Undergraduate Mathematics Series, 2001.

QUESTION PAPER PATTERN

Code number: MT 0125

Title of the paper: Differential Geometry

Paper Pattern: Students will have to answer 5 out of 7 main questions. Each main question will be worth a total of 10 marks.

The end semester question paper will have a weightage of 35% of the questions from the first half of the syllabus (the portions covered for the mid-semester examination) and a weightage of 65% of the questions from the second half of the syllabus (the portions not covered for the mid-semester examination).

Course Outcomes: At the end of the Course, the Student should

CO1	Be able to understand the concept of curvature of a curve and conditions for the planarity of a curve.
CO2	Be able to characterize all the isometries of the usual Euclidean three dimensional space.
CO3	Be equipped with various differential geometry techniques that can be applied to study the concept of congruence of curves.
CO4	Be able to analyze the shape of a given surface using the concepts of various kinds of curvatures on a surface and the concept of shape operators.

Semester	**IV**
Paper Code	**MT 0222**
Paper Title	**Fluid Mechanics**
Number of teaching hours per week	04
Total number of teaching hours per semester	60
Number of credits	04

Objective of the Paper:
To learn the concept of fluid mechanics in detail. Different methods to obtain the critical Rayleigh number value for convection.

Syllabus:
Unit 1:
Types of fluid and fluid flow. Stress tensor for a non-viscous fluid. Navier-Stokes equation. Equation of motion: Euler's equation of motion, Bernoulli's equation of motion and Bernoulli's equation for real fluid. Velocity potential function, stream function, equipotential Line and relation between stream function and velocity potential function. Motion in two-dimension, complex potential, Cauchy-Riemann equation in polar form, magnitude of velocity, sources and sinks, complex potential due to a source. Blasius theorem

20 hours

Unit 2:
Exact solution of Navier-Stokes equation: Plane Poiseuille flow, Couette flow, Hagen-Poiseuille flow and flow between two concentric rotating cylinders.

10 hours

Unit 3:
Dimensional homogeneity, similitude, dynamical similarity, inspection analysis, dimensional analysis and Model analysis. Dynamical similarity. Technique of dimensional analysis: Rayleigh's technique and Buckingham's **π**-theorem. An application of **π**-theorem to viscous compressible fluid flow.

10 hours

Unit 4:
Modes of heat transfer - conduction, convection and radiation. Steady and unsteady heat transfer. Free and forced convection. Equation of State. Boundary Conditions: on velocity and on temperature. Hydrodynamic instability (Normal mode analysis). Rayleigh-Benard convection. Galerkin Method. First variation principle. Rayleigh-Benard convection with magnetic field. 2D boundary layer equation for the flow over the flat plate. Blasius solution for boundary layer flow over a flat plate.

20 hours

TEXT BOOKS:

1. S Chandrasekar, Hydrodynamic and Hydromagnetic Stability, Dover publications, 2013.
2. R K Bansal, Fluid Mechanics and Hydraulic Machines, Laxmi publications, 10th edition, 2005.

REFERENCE BOOKS:

1. D J Tritton, Physical Fluid Dynamics, Clarendon Press, 2nd edition, 2012.
2. F Chorlton, Fluid Dynamics, CBS Publishers and Distributors, 2005.
3. P. K. Kundu, Ira M. Cohen and David R Dowling. Fluid Mechanics, Elsevier Science, 2012.
4. F. M White, Fluid Mechanics, Tata Mcgraw Hill. 2011.

QUESTION PAPER PATTERN

Code number: MT 0222

Title of the paper: Fluid Mechanics

Paper Pattern: Students will have to answer 5 out of 7 main questions. Each main question will be worth a total of 10 marks.

The end semester question paper will have a weightage of 35% of the questions from the first half of the syllabus (the portions covered for the mid-semester examination) and a weightage of 65% of the questions from the second half of the syllabus (the portions not covered for the mid-semester examination).

Course Outcomes: At the end of the Course, the Student should

CO1	Introduce and explain the fundamental concepts of Fluid Mechanics.
CO2	Understand the mechanism involved in instability that occurs during convection.
CO3	Have knowledge of dimensional analysis, equation of motion, flow between parallel plates, boundary conditions etc.
CO4	Obtain the critical Rayleigh number expression for convection problems.
CO5	Choose a relevant topic for their research.

Semester	**IV**
Paper Code	**MT 0325**
Paper Title	**Applied Stochastic Processes**
Number of teaching hours per week	03
Total number of teaching hours per semester	45
Number of credits	03

Objective of the Paper:
To introduce students to the basics of Applied Stochastic Processes.

Syllabus:

Unit 1:
Discrete-Time Markov Models: Discrete-Time Markov Chains, Transient Distributions, Occupancy Times, Limiting Behavior, First-Passage Times. Poisson Processes: Poisson Processes, Superposition of Poisson Processes, Thinning of a Poisson Process, Compound Poisson Processes.

15 Hours

Unit 2:
Continuous-Time Markov Models: Continuous-Time Markov Chains, Transient Analysis: Uniformization, Occupancy Times, Limiting Behavior, First-Passage Times. Generalized Markov Models: Renewal Processes, Cumulative Processes, Semi-Markov Processes.

15 Hours

Unit 3:
Queueing Models: Queueing Systems, Single-Station Queues, Birth and Death Queues.
Brownian Motion: Standard Brownian Motion, Brownian Motion, First-Passage Times, Martingales and Semimartingales, Black Scholes Formula

15 Hours

TEXT BOOKS:
1) V. G. Kulkarni, Introduction to modeling and analysis of stochastic systems, second edition, Springer, 2011.

REFERENCE BOOKS:
1) S. M. Ross, Stochastic processes, second edition, Wiley, 1996.
2) S. Karlin and H. M. Taylor, A first course in stochastic processes, second edition, Academic Press, 1975.
3) S. M. Ross, Introduction to Probability Models, tenth edition, Academic Press, 2009.

BLUE PRINT
Code number: MT 0325
Title of the paper: Applied Stochastic Processes

Paper Pattern: Students will have to answer 5 out of 7 main questions. Each main question will be worth a total of 10 marks.
The end semester question paper will have a weightage of 35% of the questions from the first half of the syllabus (the portions covered for the mid-semester examination) and a weightage of 65% of the questions from the second half of the syllabus (the portions not covered for the mid-semester examination).

Course Outcomes: At the end of the Course, the Student should

CO1	Define and explain fundamental concepts of stochastic processes like Markov chains, Poisson processes, Brownian motion, and renewal processes.
CO2	Differentiate between discrete-time and continuous-time stochastic processes.
CO3	Grasp the relationship between probability theory and stochastic processes.

Semester	**IV**
Paper Code	**MTDE 0425**
Paper Title	**Advanced Graph Theory**
Number of teaching hours per week	04
Total number of teaching hours per semester	60
Number of credits	04

Objective of the Paper:
To give a broader view of concepts in basic graph theory and to introduce interconnection networks and product graphs

Syllabus:

Unit 1:
Distance in Graphs : The center of a graph, Distant vertices, Locating numbers, Detour and Directed distance **,** Distance between graphs**.**

15 hours

Unit 2:
Planarity: Planar graphs, Jordan Curve theorem, Kuratowski's two graphs, Euler's polyhedral formula, detection of planarity, outer planar graphs, and other characterizations of planar graphs. Genus, thickness and crossing numbers, Dual graphs. Geometric dual, Combinatorial dual and self dual graphs.

15 hours

Unit 3:
Matching and Factorization:
Hall's theorem, matching, perfect matching, vertex/edge independence number, vertex/edge covering number, Gallali Identities. Factorization, 1-factor, 1-factorable graph, Decompositions and Graceful Labelings.

15 hours

Unit 4:
Product Graphs: Product graphs, The Cartesian Product, The Strong Product, The Direct Product, The Lexicographic Product, Properties, Distance formula, Commutativity, Associativity, Multiple Factors, Problems.
Product of Digraphs: Definitions, Connectedness, Tournaments and the Lexicographic Product.

15 hours

TEXT BOOKS:

1. G. Chartrand and Ping Zhang: Introduction to Graph Theory. McGrawHill, International edition (2005)24.
2. Narsingh Deo, Graph Theory with Application to Engineering and Computer science, Prentice Hall

of India Private Limited, New Delhi, 2016.
3. R. Hammack, W. Imrich and S.Klavzar, Handbook of product graphs, Second edition, CRC Press, A Chapman and Hall book publisher, 2011.

REFERENCE BOOKS:

1. P. Grimaldi, Discrete and Combinatorial Mathematics, 5th Edition, Pearson Education, 2004.
2. J. A Bondy and U.S.R Murty, Graph Theory with Application. London: The Macmillan Press Ltd, 1982.
3. D. B. West, Introduction to graph theory, Pearson India Education Services Pvt. Ltd., 2015.

QUESTION PAPER PATTERN
Code number: MTDE 0425
Title of the paper: Advanced Graph Theory
Paper Pattern: Students will have to answer 5 out of 7 main questions. Each main question will be worth a total of 10 marks.
The end semester question paper will have a weightage of 35% of the questions from the first half of the syllabus (the portions covered for the mid-semester examination) and a weightage of 65% of the questions from the second half of the syllabus (the portions not covered for the mid-semester examination).

Course Outcomes: At the end of the Course, the Student should

CO1	Be able to understand advances in graph theory
CO2	Have learnt a clear perspective of line graphs and its properties
CO3	Have acquired fundamental knowledge about planarity in graphs
CO4	Understand the concept of networking and select an appropriate topological structure of interconnection networks while applying it in solving real life problems using advanced graph theory
CO5	Have thorough understanding about product graphs and its properties

Semester	**IV**
Paper Code	**MTDE 0525**
Paper Title	**Number Theory**
Number of teaching hours per week	04
Total number of teaching hours per semester	60
Number of credits	04

Objective of the Paper:
To introduce some classical concepts of Basic Number Theory such as finding integer solutions of Diophantine Equations and Partition of an Integer. To understand the idea of integers in a more general setting (i.e., over any Number Field) and the idea of prime integers in any Quadratic Number Field.

Syllabus:

Unit 1:
Residue Classes and complete Residue Classes. Linear Congruences and Euler-Fermat Theorem. General Polynomial congruences and Lagrange Theorem. Wilson's Theorem. Chinese Remainder Theorem. Fundamental Theorem on Polynomial Congruences with prime power moduli. Quadratic Residue and Gauss's Law of Quadratic Reciprocity. (Both for Legendre and Jacobi symbols) Primitive roots and their existence for moduli $m = 1, 2, 4, p^{\alpha}, 2p^{\alpha}$.

20 hours

Unit 2:
Some Diophantine Equations : The Equation ax + by = c. Simultaneous Linear Equations. Pythagorean Triangles. Assorted Examples. Greatest integer function. Binary Quadratic Forms.

10 hours

Unit 3:
Results on Algebraic Number Fields. Quadratic Fields, Units in Quadratic Fields, Primes in Quadratic Fields, Unique Factorization, Primes in Quadratic Fields having Unique Factorization property, The equation $x^3 + y^3 = z^3$.

15 hours

Unit 4:
Partition: partition of a positive integer. Graphical representation. Formal Power Series, Generating functions, Euler's Identity. Introducing Simple Continued Fraction via Euclidean Algorithm. Expressing any Irrational Number as an infinite simple Continued Fraction.

15 hours

TEXT BOOKS:

1) Tom Apostol, Introduction to Analytic Number Theory, Springer, 2010.
2) Ivan Niven, Herbert. S. Zuckerman and Hugh. L. Montgomery, An Introduction to the Theory of

Numbers,
5th edition, John Wiley and Sons.

REFERENCE BOOKS:

1) André Wiel, Number theory for beginners, Springer-Verlag, 1979.
2) G H Hardy and E M Wright. An Introduction to the Theory of Numbers, Oxford University Press, 4th edition(with corrections), 1975.
3) André Wiel, Basic Number Theory, Springer-Verlag, 1995.
4) William Stein, Elementary Number Theory: Primes, Congruences, and Secrets: A Computational Approach,
Springer, 2009.

QUESTION PAPER PATTERN
Code number: MT 0525
Title of the paper: Number Theory
Paper Pattern: Students will have to answer 5 out of 7 main questions. Each main question will be worth a total of 10 marks.
The end semester question paper will have a weightage of 35% of the questions from the first half of the syllabus (the portions covered for the mid-semester examination) and a weightage of 65% of the questions from the second half of the syllabus (the portions not covered for the mid-semester examination).

Course Outcomes: At the end of the Course, the Student should

CO1	Be able to find the integer solutions of certain Diophantine Equations.
CO2	Be able to find all the primes in any Quadratic Number Field.
CO3	Be able to express any Irrational Number as an Infinite Simple Continued Fraction.
CO 4	Be able to understand the concept of Partition of a Positive Integer and some identities related to P(n).

Semester	IV
Paper Code	**MT 9R225**
Paper Title	**Project**
Number of teaching hours per week	02
Total number of teaching hours per semester	22
Number of credits	06

Objective of the Paper:
A student will choose a topic (either a research paper or continuation of the third semester topic). The student will pose a research question and investigate under the supervision of a faculty member. In the course of the semester they are required to present the progress of their work. At the end of the course they would write a dissertation.

MANNER OF EVALUATION
Code number: MT 9R225
Title of the paper: Project

Marks awarded by supervisor (90)					**Marks awarded by external examiners (60)**			**Total**
Presentation 1	Presentation 2	Final Presentation	First Draft of Master's thesis	Final Master's Thesis	Final Presentation	Master's Thesis	Viva	
20	30	20	20	20	30	30	10	150

Guidelines for students to choose NPTEL courses:

1. The student must submit a written request to the PG co-ordinator, either before the start of the semester, or within three weeks of the semester's beginning, explaining why they wish to choose the given NPTEL course.
2. The course chosen must be a PG level 3 credit course offered in Mathematics that sums for 12 weeks. It cannot be a course already part of the core courses of the regular syllabus, or an elective course that the student has already done/is doing.
3. Students with backlogs in previous semesters will not be eligible to take an NPTEL course. (Students with special permission from CoE, to miss the end sem examinations due to internships or projects are exempted from this requirement).
4. Up to 10 students will be allowed to take NPTEL courses per semester, based on merit.
5. A special committee appointed by the PG co-ordinator, consisting of the HoD, PG co-ordinator and one faculty member with NPTEL course certification will be constituted to shortlist students.
6. Students may take the desired NPTEL course, two semesters prior to the semester if they wish.
7. Students must register for the NPTEL course exam themselves.
8. Students cannot claim any reduction in their course fee at the institute.
9. The students' result will be delayed subject to any delays in declaration of NPTEL results.
10. Students will be marked absent for the course and exams connected to the institute course they wish to drop. They must get a letter signed by the PG coordinator and CoE and submit it to the welfare officer, to prevent hall ticket blockage for that semester.